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1  /*
2  Question:
3
4  1. Solve the heat diffusion equation for a rectangular plate
5  with following boundary conditions:
6
7  (i) along the left edge the temperature is given,
8  it is time independent, and changes linearly along the edge
9
10 (ii) below a constant heat flux is given
11
12 (iii) along the other two edges there is a perfect heat insulation.
13 The initial condition for temperature: linear in both coordinates
14 and satisfy boundary condition along left edge.
15
16 mathematical description:
17
18 The heat diffusion equation is .....
19  $\frac{\partial T}{\partial t} = a^2 * (\frac{\partial^2 T}{\partial x^2} + \frac{\partial^2 T}{\partial y^2})$ 
20
21 where,  $T(x,y,t)$  is temperature function .
22 and  $a^2 = k/\rho c$  is the diffusivity of a substance,
23  $k$ = coefficient of conductivity of material,
24  $\rho$ = density of the material, and
25  $c$ = specific heat capacity.
26
27  $(\frac{\partial^2 T}{\partial x^2} + \frac{\partial^2 T}{\partial y^2}) = \frac{\partial T}{\partial t}$ 
28
29 boundary conditions .... (i)  $T(0,y,t) = T_1 y$ 
30 (ii)  $T(x,0,t) = T_2$ 
31 (iii)  $T(x,y,0) = T_3 x + T_4 y$ 
32 where  $T_1, T_2, T_3, T_4$  are constants.
33
34
35  $\frac{\partial^2 T}{\partial x^2} + \frac{\partial^2 T}{\partial y^2} = 0$  ..... (T is independent of time along left to right. it becomes
Laplace equation)
36
37
38 numerical solution:
39
40 we shall assume at first that the plate is so long compared to its width that
41 we may make the mathematical approximation that
42 it extends to infinity in the y direction. It is then
43 called a semi-infinite plate. This is a good approximation if we are interested in
temperatures not too
44 near the far end.
45 The temperature T satisfies Laplace's equation
46 inside the plate where there are no sources of heat,
47 that is,
48
49  $\nabla^2 T = 0$ ,
50 OR,  $\frac{\partial^2 T}{\partial x^2} + \frac{\partial^2 T}{\partial y^2} = 0$ 
51
52 The program below for Solution of Laplace equation in C language is based
53 on the finite difference approximations to derivatives in which the
54 xy-plane is divided into a network of rectangular of sides  $\Delta x = h$ 
55 and  $\Delta y = k$  by drawing a set of lines.
56
57  $x = ih, i = 0, 1, 2, \dots$ 
58  $y = jk, j = 0, 1, 2, \dots$ 
59
60 The points of intersection of these families of lines are called mesh points,
61 lattice points or grid points.
62
63
64 */
65
66 #include<stdio.h>
67 #include<math.h>
68 #define S 4
69
70 typedef float new[ +1][ +1];
71 void (int , new )
72 {
73     int ;
74     ("n Enter the value of T[%d,i], i=1,%d\n", , );
75     for( =1; <= ; ++ )
76         ("%f", & [ ][ ] );
77 }
78 void (int , new )
79 {
80     int ;
81     ("Enter the value of T[j,%d], j=2,%d\n", , -1);
82     for( =2; <= -1; ++ )

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83         ("%f",& [ ][ ]);
84     }
85     void      (new , int , int )
86     {
87         int , ;
88         for( = ; <= ; ++ )
89         {
90             for( =1; <= ; ++ )
91                 ("%d,%d,%f", , , [ ][ ]);
92                 ("\n");
93         }
94     }
95 }
96 ()
97 {
98     new ;
99     float , , , , ;
100    int , , , , ;
101    for( =1; <= ; ++ )
102    for( =1; <= ; ++ )
103        [ ][ ]=0;
104        ("\n Enter the Boundary Condition\n");
105        (1, );      ( , );
106        (1, );      ( , );
107        (" Enter the allowed error and maximum number of iteration : ");
108        ("%f%f",& , & );
109    for( =1; <= ; ++ )
110    {
111        =0;
112        for( =2; < -1; ++ )
113        {
114            for( =2; <= -1; ++ )
115            {
116                =( [ -1][ ]+ [ +1][ ]+ [ ][ +1]+ [ ][ -1])/4;
117                = ( [ ][ ]- );
118                if( > )
119                    = ;
120                [ ][ ]= ;
121            }
122            (" Iteration Number %d\n", );
123            ( ,9,2);
124            if( <= )
125            {
126                (" After %d iteration \n The solution : \n", );
127                ( ,8,1);
128                return 0;
129            }
130        }
131    }
132    (" Sorry! The number of iteration is not sufficient");
133    return 1;
134 }
135 }
136
137 /*the constants T1,T2,T3,T4 are chosen as we want here.
138
139 OUTPUT:
140
141 Enter the Boundary Condition
142
143 Enter the value of T[1,i],i=1,4
144 10
145 10
146 10
147 10
148
149 Enter the value of T[4,i],i=1,4
150 10
151 5
152 0
153 0
154 Enter the value of T[i,1],i=2,3
155 20
156 20
157 Enter the value of T[i,4],i=2,3
158 5
159 0
160 Enter the allowed error and maximum number of iteration : 0.1
161 1
162 Iteration Number 1
163
164 Sorry! The number of iteration is not sufficient
165
166

```

